Polygons and Quadrilaterals

Chapter Review Form A

Circle the best answer.

1. Which term does NOT describe the figure?



- A concave C polygon
- B hexagon D regular

2. What is the sum of the measures of the interior angles of a 5-sided convex polygon?

- A 72 C 540
- B 360 D 900
- 3. What is the value of a?



A 60

B 80

- 4. The diagonals of *ABCD* intersect at *X*. Which is NOT true?
 - $\mathsf{A} \ \angle \textit{DAB} \cong \angle \textit{BCD}$
 - $B m \angle DAB + m \angle CBA = 180^{\circ}$
 - $\mathsf{C} \ \overline{\mathit{BC}} \cong \overline{\mathit{AD}}$
 - $\mathsf{D} \ \overline{\mathsf{A}\mathsf{X}} \cong \overline{\mathsf{X}\mathsf{B}}$

Use the figure for Exercises 5 and 6.



- 5. WXYZ is a parallelogram. Which is
 - m∠*W*?
 - A 68°
 - B 112°
- 6. WXYZ is a parallelogram. What is the value of x?
 - Α7
 - B 10

7. Which MUST be a parallelogram?



A Figure 1

B Figure 2

8. If $\overline{EF} \parallel \overline{GH}$, what additional information would allow you to conclude that EFGH is a parallelogram?



 $\mathsf{A} \ \overline{\textit{EF}} \cong \overline{\textit{GH}}$

 $\mathsf{B} \ \overline{FG} \cong \overline{EH}$

9. Which is NOT always true?

A A square is a rhombus.

B A rectangle is a parallelogram.

C A rhombus is a rectangle.

D A square is a rectangle.

10. *PQRS* is a rectangle. PR = 26. What is the value of *x*?



A 6.5 B 13

11. JKLM is a rhombus. If $m \angle JML = 70^{\circ}$, what is the value of $m \angle JKM$?



A 35°

B 55°

C 70°

D 110°

12. Given: ABCD is a parallelogram,

 $\overline{AC} \perp \overline{BD}$, and $\overline{AB} \cong \overline{CD}$.

Conclusion: *ABCD* is a square. What can be said about the conclusion?



A Valid

B Not valid

13. Which statement is needed to prove *DEFGH* is a rectangle?



A $\overline{EG} \perp \overline{HF}$

 $\mathsf{B} \ \overline{\textit{EG}} \cong \overline{\textit{HF}}$

14. Which best describes the figure?



A kite

- B parallelogram
- C quadrilateral
- D trapezoid
- 15. What is $m \angle F$ in the isosceles trapezoid?



A 79°

B 101°

16.In trapezoid PQRS, what is the length of midsegment \overline{XY} ?



A 48 cm

B 51 cm

Polygons and Quadrilaterals

Chapter Review Form B

Circle the best answer.

1. Which best describes the figure?



- A regular convex heptagon
- B irregular convex heptagon
- C irregular concave heptagon
- D irregular convex hexagon

2. What is the measure of each interior angle in a regular convex nonagon?

- F 40° H 180°
- G 140° J 1260°

3.What is the value of a?



A 2 C 180 B 90 D Not here

4. The diagonals of *ABCD* intersect at *X*. Which is always true?

- $\mathsf{F} \ \overline{BX} \cong \overline{XD}$
- $\mathsf{G} \ \overline{\mathsf{AX}} \cong \overline{\mathsf{XB}}$
- $\mathsf{H} \ \angle A \cong \angle D$
- $J m \angle A + m \angle C = 180^{\circ}$

5. In $\Box DEFG$, what is \overline{EG} ?



A 25	C 50
B 30	D Not here

6. In $\square JKLM$, what is the value of $m \angle K$?



F	15°	Н	65°
G	57°	J	115°

7. $\overline{QR} \parallel \overline{ST}$. Which additional information is NOT enough to conclude that QRST is a parallelogram?



A	$\overline{RS} \parallel \overline{QT}$	С	$\overline{QR}\cong\overline{ST}$

 $\mathsf{B} \ \overline{RS} \cong \overline{\mathsf{QT}} \qquad \mathsf{D} \ \angle \mathsf{Q} \cong \angle \mathsf{S}$

8. Which of the quadrilaterals MUST be parallelograms?



F A only H Neither A nor B

G B only J Both A and B

9.Which is NOT always true?

- A The diagonals of a rectangle divide the rectangle into four nonoverlapping isosceles triangles.
- B The diagonals of a square divide the square into four nonoverlapping right triangles.
- C The longer diagonal of a rhombus is perpendicular to two sides of the rhombus.
- D The sum of the lengths of the diagonals of a rhombus is less than the perimeter of the rhombus.

10. *WXYZ* is a rectangle. Which is NOT an expression for \overline{WT} ?



F 5x + 18 H 10x - 12

G 7x + 6 J 12x - 10

11. Which set of numbers could be the measures of $\angle DAB$, $\angle ACB$, and $\angle DBC$, respectively?



A 114°, 57°, 32.5°

B 115°, 32.5°, 57.5°

C 116°, 57.5°, 32.5°

D 117°, 58.5°, 31.5°

12. What additional information would allow you to conclude that JKLM is a rhombus?



F $\overline{JK} \parallel \overline{ML}$ and $\overline{JM} \parallel \overline{KL}$.

 $\mathsf{G} \ \overline{JM} \cong \overline{JK}$

H \overline{JL} and \overline{MK} bisect each other.

 $J \ \overline{JL} \cong \overline{MK}$

13. Which is the best name for the quadrilateral with vertices at (2, 2), (5, -2), (1, -5), and (-2, -1)?

A parallelogram C rhombus

B rectangle D square

14. In kite *UVWX*, $m \angle XUV = 84^\circ$, and $m \angle WVX = 68^\circ$. What is $m \angle VWX$?



F 22° H 44°

G 42° J 45°

15.GE = 5x + 2 and DF = 8x - 7. What is GE?



A 16

B 17

C 18

D 19

16. In trapezoid *PQRS*, if \overline{YX} is the midsegment, what could be the lengths of \overline{PQ} and \overline{SR} ?



F 4 cm and 8 cm

G 9 cm and 15 cm

H 17 cm and 31 cm

J 18 m and 30 m

Polygons and Quadrilaterals Chapter Review Form A

1. Write *True* or *False*. The figure is a regular polygon.



2. Find the sum of the measures of the interior angles of the polygon.



3. Find the measure of each exterior angle of a regular quadrilateral.

4. Write *True* or *False*. If $\overline{AB} \parallel \overline{CD}$, then *ABCD* is a parallelogram.

Use the figure for Exercises 5 and 6.



- 5. *ABCD* is a parallelogram. Find the value of *x*.
- 6. ABCD is a parallelogram. Find m $\angle C$.
- 7. Write True or False. The quadrilateral is a parallelogram.



8. In the figure, $\overline{JM} || \overline{KL}$. Show that the quadrilateral is a parallelogram for x = 3.



- 9. Write True or False. A square is a rhombus.
- 10. ABCD is a rectangle. AD = 15, AC = 25, and DC = 20. Find BD.



11. *RSTU* is a rhombus. $m \angle SRU = 112$. Find $m \angle TRU$.



12. Write *True* or *False*. If $\overline{EF} || \overline{HG}$ and $\overline{EH} || \overline{FG}$, then $\Box EFGH$ is a rectangle.



13. **Given:** UVWX is a parallelogram and $\overline{UV} \cong \overline{XU}$.

Conclusion: *UVWX* is a rhombus. Determine whether the conclusion is valid.



14. In kite *JKLM*, $m \angle JMN = 25^{\circ}$. Find $m \angle NJM$.







16. Find the length of the midsegment of trapezoid PQRS.



Polygons and Quadrilaterals

Chapter Review Form B

1. Name the polygon by its number of sides and tell whether it is regular or irregular.



- 2. Find the measures of each interior angle of a regular octagon.
- 3. Find the value of a.



4. Write a biconditional statement to define the term parallelogram.

5.ABCD is a parallelogram. Find AB and BX.



6. *EFGH* is a parallelogram. Find $m \angle E$.



7. Write *True* or *False*. The quadrilateral must be a parallelogram.



8. Show that *JKLM* is a parallelogram for x = 7 and y = 14.



- 9. Complete the sentence. A _____ is a parallelogram that has the properties of both a _____ and a
- 10. *ABCD* is a rectangle with diagonals \overline{BD} and \overline{AC} that intersect at *X*. BD = 12x - 6 inches and AX = 4x + 5 inches. Find *DX*.

11. *RSTQ* is a rhombus. Find $m \angle PST$.



12. **Given:** WXYZ is a parallelogram. \overline{WY} and \overline{XZ} bisect each other and

 $\overline{WY} \perp \overline{XZ}$.

Conclusion: *WXYZ* is a rectangle. Determine whether the conclusion is valid. If not, tell why not.

13. Tell whether the parallelogram is a rectangle, rhombus, or square.

	G(-	4, 3)	3-	y		
	/				D(2,	1) x
F(-5	, 0)				2	>
			-3	E	(1, -	-2)

14. In kite *JKLM*, $m \angle LMN = 25^{\circ}$, and $m \angle LKN = 43^{\circ}$. Find $m \angle MLK$.



15. In trapezoid *ABCD*, find $m \angle A$.



16. \overline{XY} is the midsegment of trapezoid *ABCD*. Find *AB*.



Chapter Review Form A: Multiple Choice

1. D	9. C
2. C	10. A
3. A	11. A
4. D	12. B
5. A	13. B
6. A	14. A
7. B	15. A

8. A 16. A

Chapter Review Form B: Multiple Choice

1. C	9. C
2. G	10. J
3. A	11. D
4. F	12. G
5. C	13. D
6. H	14. H
7. B	15. B
8. J	16. H

Chapter Review Form A: Free Response

- 1. True
- 2. 540°
- 3. 90°
- 4. False
- 5. 11
- 6.66°
- 7. True
- 8. Find JM and KL.

JM = 5x - 1 and KL = 3x + 5 Given JM = 5(3) - 1 = 14 Subst. and simplify. KL = 3(3) + 5 = 14 Subst. and simplify. Since JM = KL and $\overline{JM} \parallel \overline{KL}$, JKLM is a parallelogram by Theorem 6-3-1.

- 9. True
- 10. 25
- 11. 56°
- 12. True
- 13. valid
- 14. 65°
- 15. 104°
- 16. 72

Chapter Review Form B: Free Response

- 1. irregular hexagon
- 2. 135°
- 3. 120°
- 4. A quadrilateral is a parallelogram if and only if it has two pairs of parallel sides.
- 5. *AB* = 30; *BX* = 25
- 6. 70°
- 7. True
- 8. $m \angle J = (9y + 1)^\circ = [9(14) + 1]^\circ = 127^\circ; m \angle L$ = $(10y - 13)^\circ = [10(14) - 13]^\circ$ = $127^\circ; m \angle K = (7x + 4)^\circ = [7(7) + 4]^\circ$ = $53^\circ;$ Since $127^\circ + 53^\circ = 180^\circ, \angle K$ is supplementary to both $\angle J$ and $\angle L$. *JKLM* is
- a parallelogram by Theorem 6-3-4.
- 9. square; rhombus; rectangle
- 10. 21 in.
- 11. 33°
- 12. Not valid; possible answer: conditions for a rectangle are 1 ∠ of a □ is a rt.
 ∠ or the diagonals of a □ are ≃. While the quadrilateral is a □ and a rhombus, neither of the conditions for a rectangle are met.
- 13. Sample answer:

$$DF = \sqrt{[2 - (-5)]^2 + (1 - 0)^2}$$
$$= \sqrt{7^2 + 1^2} = \sqrt{50} = 5\sqrt{2}$$
$$EG = \sqrt{[1 - (-4)]^2 + [(-2) - 3]^2}$$
$$= \sqrt{5^2 + (-5)^2} = \sqrt{50} = 5\sqrt{2}$$

The diagonals are congruent so by Theorem 6-5-2, *DEFG* is a rectangle.

slope of
$$\overline{DF} = \frac{1-0}{2-(-5)} = \frac{1}{7}$$

slope of $\overline{EG} = \frac{-2-3}{1-(-4)} = \frac{-5}{5} = 1$

 $\left(\frac{1}{7}\right)$ (1) \neq -1, so \overline{DF} is not perpendicular to \overline{FG} .

So *DEFG* is not a rhombus and therefore cannot be a square. *DEFG* is a rectangle.

- 14. 112°
- 15. 104°
- 16. 48